



SCHOOL	ENGINEERING AND THE BUILT ENVIRONMENT		
DEPARTMENT	ELECTRICAL AND COMPUTER ENGINEERING		
SUBJECT	CONTROL ENGINEERING		
SUBJECT CODE	TECP3891		
DATE	MAY/JUNE 2024		
DURATION	3 HRS	MARKS	100

First Opportunity Examination

Examiner: DR. T. WANJEKECHE

Internal Examiner: MR. F. PHIRI

External Moderator: PROF. J. TSADO

This question paper consists of **5** pages excluding this front page.

Instructions

1. Closed book examination.
2. Read the questions carefully
3. Answer **5 questions** out of 6 questions
4. Marks for each question are indicated
5. Start each question on a fresh paper
6. Additional materials: None

QUESTION 1 [20]

1.1 A system is critically damped. How will the system behave, if the gain of the system is increased? [2]

1.2 Consider the closed loop system shown in Fig. Q 1.2. where z and p are real numbers.

1.2.1 Find the set of values of z and p such that the feedback loop is BIBO stable. Draw the range of values of p and z (*Hint: Take values of p and z to be on the y and x -axis respectively*) [7]

1.2.2 Assume $D(s) = 0$. Find the set of values of z and p such that the closed-loop system achieves the following transient specifications to a step input: settling time $T_s \leq 4\text{sec}$, $\%OS \leq 1\%$. Draw the range of values of p and z (*Hint: Take values of p and z to be on the y and x -axis respectively*) [11]

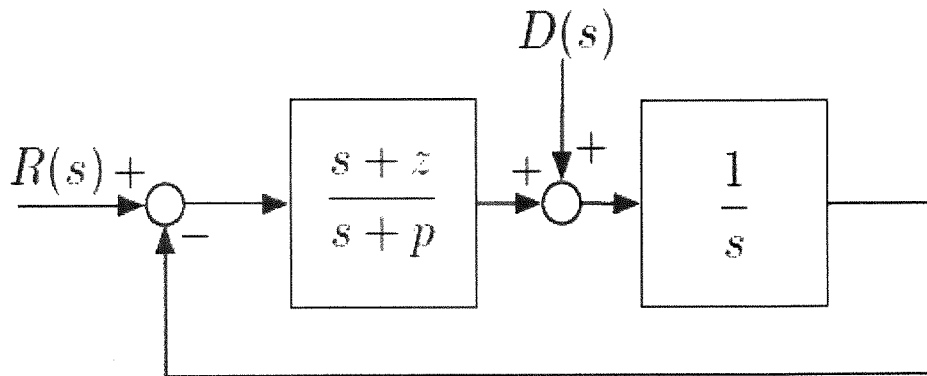


Fig. Q 1.2

QUESTION 2 [20]

For the system shown in Fig. Q. 2:

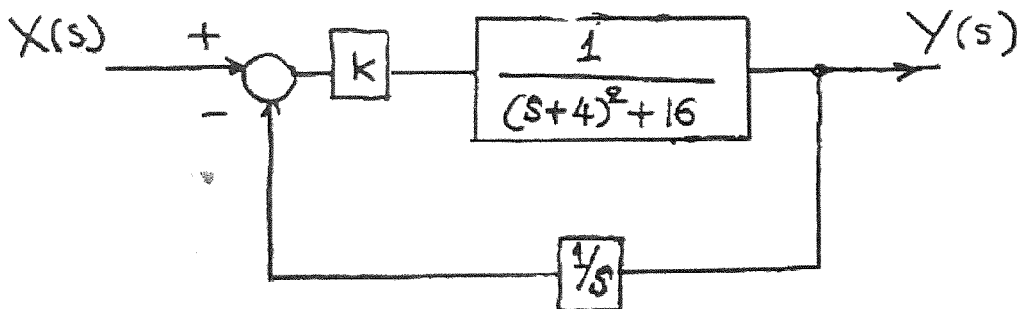


Fig. Q. 2

- 2.1 Draw a root locus for this system. Determine and indicate any departure angles, asymptote intersection and break away points [12]
- 2.2 Find the range of K for stability of the system [5]
- 2.3 Determine the point where the root loci cross the imaginary axis and the corresponding value of K [3]

QUESTION 3 [20]

- 3.1 Define the term Robust stability. Using equations explain how a polynomial $P(s)$ is robust Stable [8]
- 3.2 There are two performance factors for a first-order differential equation. What are they? Explain what each factor means in terms of response of the system [5]
- 3.3 Fig. Q. 3.3 shows unit step response of a system $G(s)$, determine its transfer function [7]

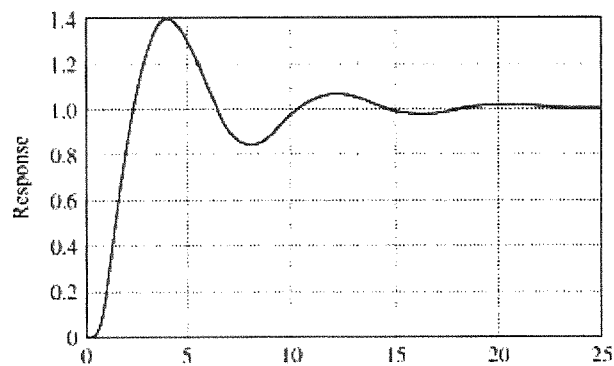


Fig. Q. 3.3

QUESTION 4 [20]

- 4.1 For the Electrical network shown in Fig.Q.4.1:

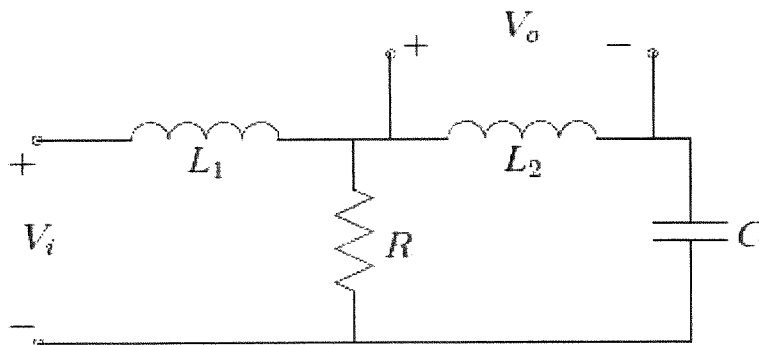


Fig.Q.4.1

- 4.1.1 Derive its mathematical model in Laplace transform (S- Domain) [3]
- 4.1.2 Using equations in 4.1.1. determine the state and output equations of the system in a Vector- matrix form [7]
- 4.2 Write the state equations in vector matrix of the control system with the prespecified state variables in the Fig Q.4.2 [10]

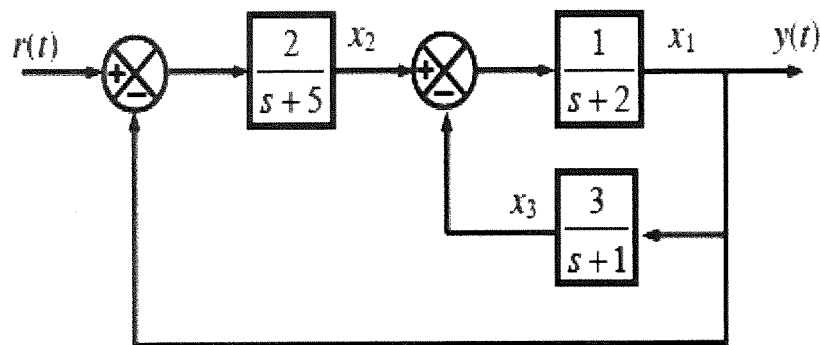


Fig. Q 4.2

QUESTION 5 [20]

- 5.1 State 3 (THREE) reasons why modeling a physical system is important in control system [3]
- 5.2 List 3 (THREE) advantages of Block diagram reduction as a techniques of modelling dynamic systems [3]
- 5.3 Obtain the transfer functions $X_1(s)/F(s)$ of the mechanical system shown in Fig. Q.5.3. [8]

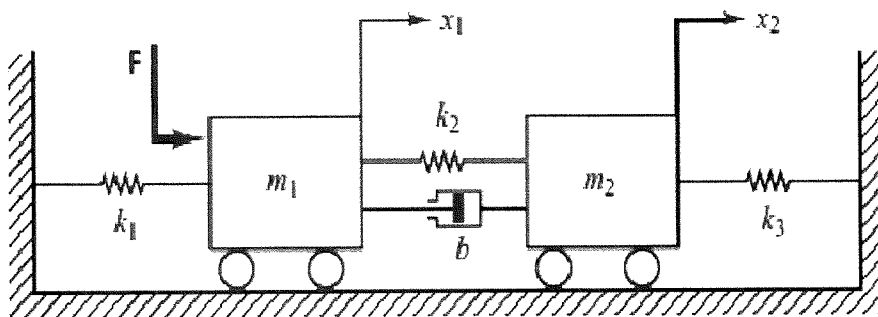


Fig. Q.5.3

5.4 Obtain a closed loop transfer function of the system in **Fig.5.4**. Select the gain K_1 and K_2 so that the closed loop system is critically damped with two equal poles at $s = -10$ [6]

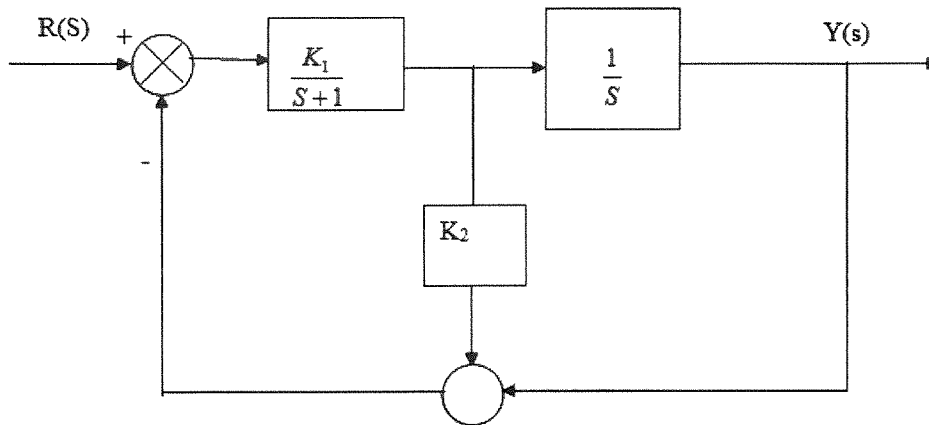


Fig. Q.5.4

QUESTION 6 [20]

6.1 A Control System is having a percentage overshoot of 40%, and the production manager is recommending a PI Controller to reduce the overshoot to 20%, as a Control System Engineer will you recommend the PI controller? Justify your answer. [3]

6.2 Derive the closed loop equation of PI controller with a first order plant, and show that the natural frequency ω_n and damping ratio ζ can be controlled independently for a unit step input [7]

6.3 **Fig. Q. 6.3** Shows a closed loop system with transfer function

$$G_P = \frac{1}{s(s+2)}$$

You are required to design a controller $G(s)$ so that the closed loop system meets the following specifications:

1. The damping ratio of the dominant be $\zeta = 0.45$
2. The velocity error constant must be $K_V = 0.20$

6.3.1 Using proportional controller $G_c(s) = K$, determine the value of K to receive to achieve the desired closed loop state steady accuracy requirement [2]

- 6.3.2 Using the proportional controller in 6.3.1, determine the damping ratio of the dominant closed loop poles. Can we achieve both specifications using proportional controller, K ? Justify your answer [8]

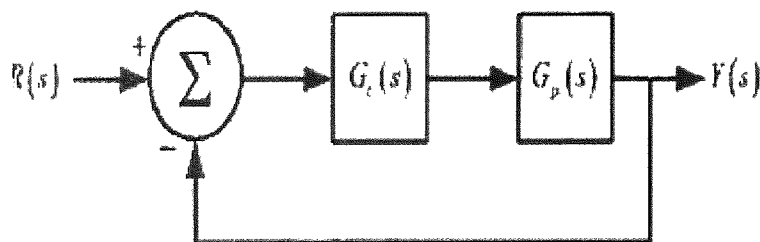


Fig. Q. 6.3